

Solving Equations
Emphasis on Multi-Step Linear Equations

Solve each of the following.

1. $p + 2p - 3 = 6$

$$\begin{array}{r} 3p - 3 = 6 \\ +3 \quad +3 \end{array}$$

$$\frac{\cancel{3}p}{\cancel{3}} = \frac{9}{3}$$

$$p = 3$$

2. $12v + 14 + 10v = 80$

$$\begin{array}{r} 22v + 14 = 80 \\ -14 \quad -14 \end{array}$$

$$\frac{\cancel{22}v}{\cancel{22}} = \frac{66}{22}$$

$$v = 3$$

3. $11w - 9 - 7w = 15$

$$\begin{array}{r} 4w - 9 = 15 \\ +9 \quad +9 \end{array}$$

$$\frac{\cancel{4}w}{\cancel{4}} = \frac{24}{4}$$

$$w = 6$$

4. $5a + 3 - 3a = -7$

$$\begin{array}{r} 2a + 3 = -7 \\ -3 \quad -3 \end{array}$$

$$\frac{\cancel{2}a}{\cancel{2}} = \frac{-10}{2}$$

$$a = -5$$

5. $6c - 8 - 2c = -16$

$$\begin{array}{r} 4c - 8 = -16 \\ +8 \quad +8 \end{array}$$

$$\frac{\cancel{4}c}{\cancel{4}} = \frac{-8}{4}$$

$$c = -2$$

6. $9 = 7z - 13z - 21$

$$\begin{array}{r} 9 = -6z - 21 \\ +21 \quad +21 \end{array}$$

$$\frac{30}{-6} = \frac{\cancel{-6}z}{\cancel{-6}}$$

$$z = -5$$

7. $-2 = 3y - 18 - 5y$

$$\begin{array}{r} -2 = -2y - 18 \\ +18 \quad +18 \end{array}$$

$$\frac{16}{-2} = \frac{\cancel{-2}y}{\cancel{-2}}$$

$$y = -8$$

8. $23 = -4m + 2 + m$

$$\begin{array}{r} 23 = -3m + 2 \\ -2 \quad -2 \end{array}$$

$$\frac{21}{-3} = \frac{\cancel{-3}m}{\cancel{-3}}$$

$$m = -7$$

9. $3 + 4(z + 5) = 31$

$$3 + 4z + 20 = 31$$

$$\begin{array}{r} 23 + 4z = 31 \\ -23 \quad -23 \end{array}$$

$$\frac{\cancel{4}z}{\cancel{4}} = \frac{8}{4}$$

$$z = 2$$

10. $14 + 2(4g - 3) = 40$

$$14 + 8g - 6 = 40$$

$$\begin{array}{r} 8 + 8g = 40 \\ -8 \quad -8 \end{array}$$

$$\frac{\cancel{8}g}{\cancel{8}} = \frac{32}{8}$$

$$g = 4$$

$$11. 5m + 2(m + 1) = 23$$

$$5m + 2m + 2 = 23$$

$$7m + 2 = 23$$

$$\frac{7m}{7} = \frac{21}{7}$$

$$m = 3$$

$$12. 5h + 2(11 - h) = -5$$

$$5h + 22 - 2h = -5$$

$$3h + 22 = -5$$

$$\frac{3h}{3} = \frac{-27}{3}$$

$$h = -9$$

$$13. 27 = 3c - 3(6 - 2c)$$

$$27 = 3c - 18 + 6c$$

$$27 = 9c - 18$$

$$\frac{45}{9} = \frac{9c}{9}$$

$$c = 5$$

$$14. -3 = 142y - 5(2y - 7)$$

$$-3 = 142y - 10y + 35$$

$$-3 = 132y + 35$$

$$\frac{-38}{132} = \frac{132y}{132}$$

$$y = \frac{-19}{66}$$

$$15. 7v - (6 - 2v) = 12$$

$$7v - 6 + 2v = 12$$

$$9v - 6 = 12$$

$$\frac{18}{9} = \frac{18}{9}$$

$$v = 2$$

$$16. \frac{1}{3}(d + 3) = 5$$

$$\frac{1}{3}d + 1 = 5$$

$$\frac{3}{1} \left[\frac{1}{3}d = 4 \right] \frac{3}{1}$$

$$d = 12$$

$$17. \frac{3}{2}(x - 5) = -6$$

$$\frac{3}{2}x - \frac{15}{2} = -6$$

$$\frac{3}{2}x = \frac{3}{2}$$

$$x = 1$$

$$18. \frac{4}{3}(7 - n) = 12$$

$$\frac{3}{4} \left[\frac{4}{3}(7 - n) = 12 \right] \frac{3}{4}$$

$$7 - n = 9$$

$$-n = 2$$

$$n = -2$$

$$19. 4 = \frac{2}{9}(4y - 2)$$

$$4 = \frac{8}{9}y - \frac{4}{9}$$

$$\frac{40}{9} = \frac{8}{9}y$$

$$\frac{40}{8} = \frac{8}{8}y$$

$$y = 5$$

$$20. -32 = \frac{8}{7}(3w - 1)$$

$$\frac{7}{8} \left[-32 = \frac{8}{7}(3w - 1) \right] \frac{7}{8}$$

$$-28 = 3w - 1$$

$$\frac{-27}{3} = \frac{8w}{3}$$

$$w = -9$$

Alternate Method

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